

# Nucleosynthesis induced by the Fast Accretion of sMBH in the Disk of AGN

## Thesis Defence

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# Explanation of the high metallicity of AGN

- Observational evidence shows the exceptional super-solar metallicity in the broad line region (BLR) of AGN<sup>[10]</sup>.

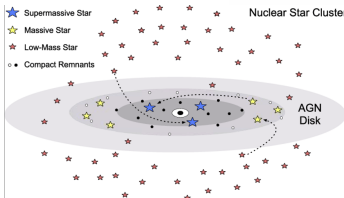


Fig. 1: <sup>[1]</sup>Hypo. 1: Capturing from the nuclear star cluster.



Fig. 2: <sup>[9]</sup>Hypo.2 Star formation, evolution result

- Either way, they finally grow to massive BH. High accretion rate ( $\sim 10^9 L_{\text{Edd}}/c^2$ ), high density ( $\sim 10^{14} \text{cm}^{-3}$ ). AMS may bring a new view to explain the nature of AGN

# Our goal

- Modified the model of the fast accretion onto BH.(advection dominated, hot flow)
- Calculated the abundances after the nucleosynthesis in the disk.

# Basic equations (After vertically integrated)

- Continuity equation

$$\frac{\partial \Sigma}{\partial r} = -\frac{\Sigma}{r} - \frac{\Sigma}{v} \frac{\partial v}{\partial r}, \quad (1)$$

- Equation of motion (origins from Navier-Stokes Equation)

$$v_r \frac{dv_r}{dr} + \frac{1}{\Sigma} \frac{d\Pi}{dr} = \frac{\ell^2 - \ell_K^2}{r^3} - \frac{\Pi}{\Sigma} \frac{d \ln \Omega_K}{dr},$$

$$\dot{M}(\ell - \ell_{\text{in}}) = -2\pi r^2 T_{r\varphi}, \quad (2)$$

$$\Omega_K^2 H^2 = (2N + 3) \frac{\Pi}{\Sigma}.$$

- Energy Equation

$$Q_{\text{vis}}^+ + \boxed{Q_{\text{nuc}}^+} = Q_{\text{adv}}^- + Q_{\text{rad}}^-, \quad (3)$$

- Equation of state

$$p = \text{ideal gas} + \text{radiation} + \cancel{\text{degenerate}}. \quad (4)$$

# Nuclear Reaction<sup>[2]</sup>: H and He burning

- H burning

- p-p chain reaction,  $T \in [1.5, 1.8] \times 10^7 \text{K}$ ,

$$R_{\text{pp}} \propto \rho X^2 T^4. \quad (5)$$

- CNO cycle,  $T > 1.8 \times 10^7 \text{K}$ ,

$$R_{\text{CNO}} \propto XX_{\text{CNO}} \rho T^{18}. \quad (6)$$

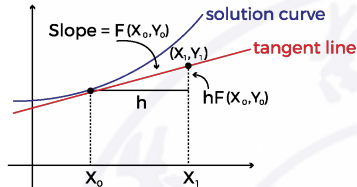
- He burning,  $T > 10^8 \text{K}$ .

$$R_{3\alpha} \propto Y^3 \rho^2 T^{40}. \quad (7)$$

The specific expressions are not shown because they are so long.

# Method

- Euler's Method



Calcworkshop.com

Fig. 3: Euler's Method

- Initial condition
  - adjust the inner angular momentum to show the transonic nature of BH accretion.
  - Keplerian rotation.

# Result (1): Thermodynamics

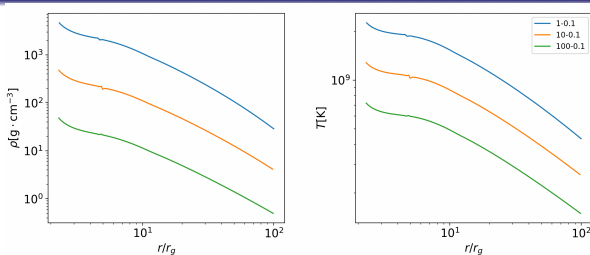


Fig. 4: Fix  $\dot{M}/\dot{M}_{\text{edd}} = 10^8$ , the profile of  $T$  and  $\rho$ . Higher BH mass gives a low temperature and density.

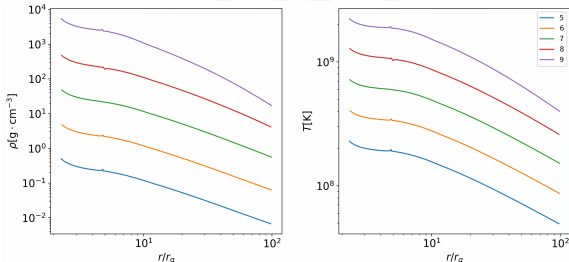


Fig. 5: Fix  $M_{\text{BH}} = 10M_{\odot}$ , the profile of  $T$  and  $\rho$ . Higher accretion rate gives a higher temperature and density.

# Thermal instability analysis

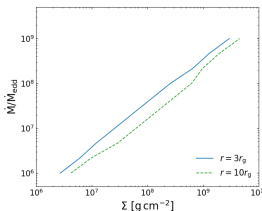


Fig. 6: Phase Diagram on  $\dot{M} - \Sigma$ .  
The slope is always positive.

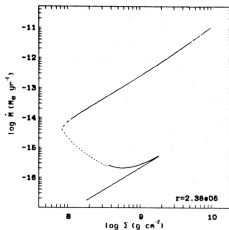


Fig. 7: [7] Phase diagram of a White dwarf

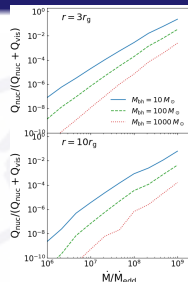


Fig. 8: Ration of the endothermic rate of Nuclear reaction

No thermal instability:

- If the viscosity is normal ( $\alpha \sim 10^{-1}$ ),  $Q_{\text{nuc}} \ll Q_{\text{vis}} \approx Q_{\text{adv}}$ .
- Even if  $Q_{\text{nuc}} \geq Q_{\text{vis}}$  (by dropping  $\alpha$ ), the benefit is balanced out by high advection cooling.  
The NS and WD: a *real edge*, a nuclear burst<sup>[7][3][6]</sup>;  
But BH: no *counterpart*.

Reemphasize: advection cooling is one of the two most important nature of BH accretion (Kato<sup>[5]</sup>).



## Result (2): Nuclear Network

- We calculated the abundances of  $^{12}\text{C}$ ,  $^{14}\text{N}$ ,  $^{16}\text{O}$  and other species after 1s using an open-source FORTRAN code [8][4].

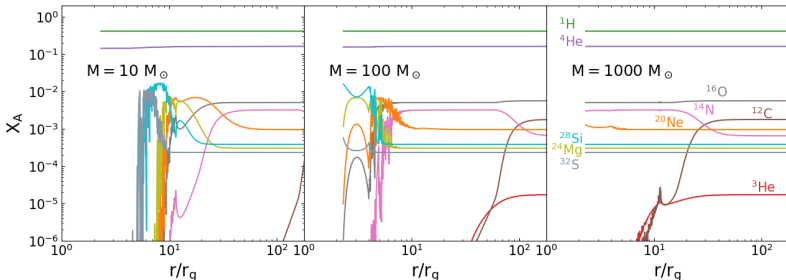


Fig. 9: The profile of mass fraction of Elements after 1s. Carbon and/or Nitrogen was depleted in the inner region, causing the increase of metallicity.

Tab. 1: The metal abundances in the Sun

O	C	Ne	N	Si	Mg	S
$7 \times 10^{-3}$	$2.9 \times 10^{-3}$	$10^{-3}$	$9 \times 10^{-4}$	$7 \times 10^{-4}$	$5 \times 10^{-4}$	$4 \times 10^{-4}$

# Ration of C, N, and O

- We drew N/C and O/C at  $5r_g$  and  $10r_g$ . Indicators of metallicity in observations.

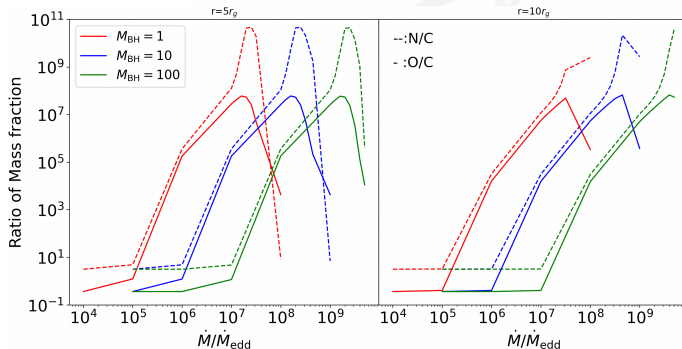


Fig. 10: O/C and N/C with respect to  $\dot{M}$  at  $5r_g$  and  $10r_g$  after 1s. Roughly speaking, higher accretion rate brings higher ratio because of the higher  $T$  and  $\rho$ . We could not explain the peaks and their shifts til now.

# Conclusion

- Disk thermodynamics
  - The structure of the disk of AMSs is modeled and numerically solved.
  - The increase of  $\dot{M}$  and the decrease of  $M_{\text{BH}}$  brings a higher  $\rho$  and  $T$ . But does not make it thermally unstable or degenerate.
- Nuclear network
  - The nucleosynthesis is examined using an open-source, 19-species nuclear network FORTRAN code.
  - Prominent metal enrichment happened in the disk.  $^{12}\text{C}$  was depleted in the inner region of the disk ( $\leq 10^1 r_g$ ), subsequently causing the increase of  $^{14}\text{N}$ ,  $^{20}\text{Ne}$ ,  $^{24}\text{Mg}$ ,  $^{28}\text{Si}$  and  $^{20}\text{S}$ .
- Outlook
  - The peak and the successive drop cannot be interpreted. (Numerical issue?)
  - Transform the mass ratio to the fluxes of the emission line.

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*Thanks!*

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